

## Algorithms of Scientific Computing II

### Exercise 4 - Methods for Long-Range Potentials

#### 1) Error estimation

In this exercise we want to analyse the error in the calculation of long-range potentials with the tree methods from the lecture. Assume, that the kernel  $G$  of the potential  $\Phi$  behaves like a  $\frac{1}{r}$ -potential.

In the lecture it was stated, that the relative local approximation error in the calculation of  $\Phi$  is  $O(\theta^{p+1})$ . Prove that!

Use the  $\theta$ -criterion from the lecture:

$$\frac{diam}{\|x - y'_0\|} \leq \theta$$

#### 2) Complexity of the Barnes-Hut-Method

In the lecture the costs for the d-dimensional Barnes-Hut-Method were given as  $O(\theta^{-d}N \log N)$ . First derive the costs for the twodimensional Barnes-Hut-Method. Then explain descriptively (without proof), why the formula is also correct for 3d.