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High Performance Computing - Programming Paradigms and Scalability

Exercise Sheet 6: MPI

1 Parallel Summation

For the parallel summation of N^2 integers a 2–dimensional torus of size $N \times N$ is to be used. Each node of the torus is initialised with the integer value `val = rank + 1`. The parallel summation works as follows:

```
1   sum = val;
2   tmp = val;
3
4   for(i = 1; i < N; i++) {
5       MPI_send(tmp, 1, MPI_INT, left neighbour, ...);
6       MPI_recv(tmp, 1, MPI_INT, right neighbour, ...);
7       sum = sum + tmp;
8   }
9
10  tmp = sum;
11
12  for(i = 1; i < N; i++) {
13      MPI_send(tmp, 1, MPI_INT, lower neighbour, ...);
14      MPI_recv(tmp, 1, MPI_INT, higher neighbour, ...);
15      sum = sum + tmp;
16  }
```

a) Describe how the program works for a 3×3 torus by showing the content and direction of all the transfered messages for each computational step of the algorithm.

For this purpose, $\xrightarrow{x}$ shows that value "x" is transfered from left to right and the nodes of the torus (circles) contain the current local value of `sum`.

Example: *before:* $\leftarrow\cdots$ ① $\xleftarrow{2}$ *after:* $\leftarrow\cdots$ ③ $\leftarrow\cdots$

b) Determine the number of required computation steps $T(p)$ depending only on N, neglecting communication. Use this to approximate speedup and parallel efficiency and illustrate the parallel efficiency by plotting it for different values of N. Do you notice anything peculiar, how would you rate this parallel program?

2 Collective Communication

Given is a 2-dimensional torus of size $N \times N$. Nodes are labelled from 1 to N in both dimensions where node $(1, 1)$ resides in the upper left corner and node (N, N) in the lower right corner of this topology. For implementing a broadcast, each node – after receiving – always forwards the received information both to its right and lower neighbour. This procedure – starting from one dedicated root node – successively continues until all nodes have been informed. In order to keep this procedure "symmetric", the root node should also receive from its other two neighbours.

a) Sketch the single steps of this algorithm (drawing arrows between sender and receiver nodes) for a 4×4 torus with node $(1, 1)$ as root!

b) Give an MPI implementation (a communication skeleton is enough) of the above algorithm using correct send/receive statements and also think about dependencies! To keep communication simple, you may refer to a node's neighbours with left, right, up, and down instead of MPI ranks.